

FMPC 12 1.4(a) TRANSFORMATIONS – Practice Exercises

1. x has been replaced with $x+3$

therefore, the graph is translated **3 units LEFT**

2. 2 units left means, “replace x with $x+2$ ”
4 units down means, “replace y with $y+4$ ”

The equation then becomes $y+4 = |x + 2|$

- isolate y and get

$$y = |x + 2| - 4$$

3. x has been replaced with $x-3$
 y has been replaced with $y-6$

The graph has been translated **3 units RIGHT and 6 units UP**

4. The x -coordinate has changed from 0 to -4 which means the graph is horizontally translated
4 units LEFT \rightarrow Replace x with $x+4$

The y coordinate has changed from 0 to 2 which means the graph is also vertically translated
2 units UP \rightarrow Replace y with $y-2$

$$(x+4)^2 + (y-2)^2 - 25 = 0$$

5. x has been replaced with $x-5$,

therefore, the graph has been translated **5 units RIGHT**

6. 2 units to the right means, “replace x with $x-2$ ”
5 units up means, “replace y with $y-5$ ”

So we get $y-5 = \frac{1}{x-2} \rightarrow y = \frac{1}{x-2} + 5$

7. y has been replaced with $y+4$ which means...**4 units DOWN**
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8. x has been replaced with $x-5$ which means the x -coordinates have been translated 5 units RIGHT. The x -intercept are affected as such...

$(3+5, 0)$ and $(-3+5, 0)$ which gives us new x -intercepts of **$(8,0)$ and $(2,0)$**

9. x has been replaced with $x-4$
 y has been replaced with $y-3$

The graph has been translated **4 units RIGHT and 3 units UP**

10. The vertical asymptote is the y -axis. This really means it is the vertical line $x=0$.
A vertical asymptote of $x=4$ means we would translate the graph 4 units RIGHT.
So, **replace x with $x-4$**

$$y = \frac{1}{x-4}$$

11. The corner has been horizontally translated 3-(-4) or 7 units LEFT. So,

replace x with x+7.

12. The vertices have been translated 2 units UP $(0,4) \rightarrow (0,6)$ and $(0,-4) \rightarrow (0,-2)$

Therefore, replace y with y-2 and get, $\frac{(y-2)^2}{16} - \frac{x^2}{4} = 1$

13. **B.** x has been replaced with x+2. This means, “subtract 2 from the x-coordinate”

$$(a, b) \rightarrow (a-2, b)$$

14. **B.** Because, in order to move the graph 4 units LEFT, we must **replace x with x+4**.
For a translation 2 units UP, we must **replace y with y-2**.

The equation then becomes $y-2 = f(x+4) \rightarrow y = f(x+4) + 2$ compare this to $y = f(x-a) + b$
and we can see **a= -4 and b=2**

15. **C.** For $y = (x+2)^2 + 3$ replace y with y+2 and get $y+2 = (x+2)^2 + 3$
 $y = (x+2)^2 + 3 - 2$
 $y = (x+2)^2 + 1$

16. For $y = (x-2)^2$ replace x with x-5 and get $y = ((x-5)-2)^2$

$$y = (x-5-2)^2$$

$$y = (x-7)^2$$

The value of h is 7.

17. $y-5 = (x-3)^2 - 2 \rightarrow y = (x-3)^2 - 2 + 5 \rightarrow y = (x-3)^2 + 3$

This is a parabola that opens up and has been translated 3 units UP. The vertex is now at (3,3) instead of (0,0). **The range is $y \geq 3$**