

# FMPC 10

6.1, page 236

#4a & 4c

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4a) If  $(5, 2)$  is a solution to the system then it MUST satisfy both equations

CHECK  $3x + y = 17$   $\longrightarrow$  does  $3(5) + 2 = 17$   
 $15 + 2 = 17$  YES!

now CHECK  $2x + 3y = 17$   $\longrightarrow$  does  $2(5) + 3(2) = 17$   
 $10 + 6 = 17$  NO!

$\therefore (5, 2)$  is NOT a solution to the system. This simply means that the graphs of two lines do not intersect at  $(5, 2)$

4c) Is  $(\frac{2}{x}, -\frac{4}{y})$  a solution to the linear system?

CHECK  $x + 2y = -2$   $\longrightarrow$  does  $2 + 2(-4) = -2$   
 $2 - 8 = -2$   
 $-6 = -2$  NO!

$\therefore$  since it is NOT a solution for this equation it is NOT a solution to the system.

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#4h

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$$\begin{aligned} 4h) \quad 0.3x - 0.2y &= 4 & \left(\frac{140}{13}, \frac{-50}{13}\right) \\ 0.2x + 0.3y &= 1 \end{aligned}$$

Plug the number into each equation to see if the left side equals the right side.

$$0.3 = \frac{3}{10} \quad \text{and} \quad 0.2 = \frac{2}{10}$$

$$\therefore \frac{3}{10} \left(\frac{140}{13}\right) - \frac{2}{10} \left(\frac{-50}{13}\right) = 4$$

$$\frac{42}{13} + \frac{10}{13} = 4 \quad \longrightarrow \quad \frac{42+10}{13} = 4$$

$$\frac{52}{13} = 4$$

$$4 = 4 \quad \text{TRUE}$$

$$\frac{2}{10} \left(\frac{140}{13}\right) + \frac{3}{10} \left(\frac{-50}{13}\right) = 1$$

$$\frac{28}{13} - \frac{15}{13} = 1 \quad \longrightarrow \quad \frac{28-15}{13} = 1$$

$$\frac{13}{13} = 1$$

$$1 = 1 \quad \text{TRUE}$$

$\therefore \left(\frac{140}{13}, \frac{-50}{13}\right)$  is a solution to the linear system.

# FMPC 10

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#6c

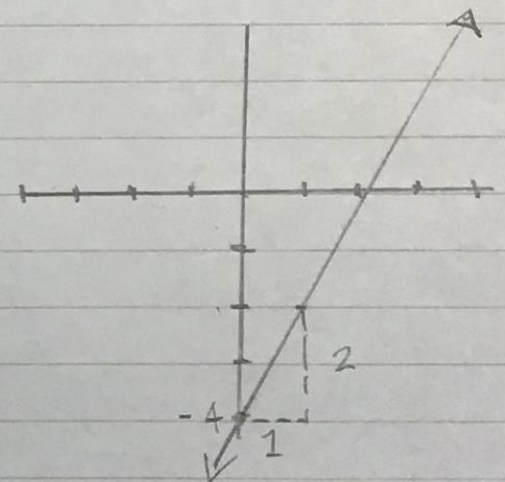
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6c) Graph both equations on the same grid.

$f(x) = 2x - 4$  is a line with a slope = 2 and a y-int = -4

$x - \frac{1}{2}y = 2$  is a line with a slope =  $-\frac{1}{-\frac{1}{2}} = 2$   
and a y-int =  $\frac{2}{-\frac{1}{2}} = -4$

Both graphs are the same line! Therefore there are an infinite number of solutions





# FMPC 10

6.2, page 243

#1b

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$$1b) \quad (3x - y = 4)$$

$$x + 2y = 2$$

The idea here is to determine a number that we can multiply the first equation by in order to eliminate one of the variables when we ADD the two equations.

In this case, we can multiply  $(3x - y = 4)$  by 2 because when we ADD the equations the y's cancel out.

$$\begin{array}{r} \text{so, } (3x - y = 4) \times 2 \longrightarrow 6x - 2y = 8 \\ \oplus \quad x + 2y = 2 \\ \hline 7x = 10 \end{array}$$

we can solve this for x and then substitute  $x = \frac{10}{7}$  into either equation and find y.

OR// we can multiply  $(3x - y = 4)$  by  $-\frac{1}{3}$  because when we ADD the equation the x's cancel out.

$$\begin{array}{r} \text{so, } (3x - y = 4) \times -\frac{1}{3} \longrightarrow -1x + \frac{y}{3} = -\frac{4}{3} \\ x + 2y = 2 \\ \hline 2\frac{1}{3}y = \frac{2}{3} \\ \frac{7}{3}y = \frac{2}{3} \\ y = \frac{2}{3} \times \frac{3}{7} = \frac{2}{7} \end{array}$$

# FMPC 10

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#2a

FMPC 10 p.243

$$2a) \quad x - y = 4$$

$$x + y = -6$$

- simply ADD these equations because we can see  $y$  will cancel out

$$x - y = 4$$

$$\underline{x + y = -6}$$

$$2x = -2 \longrightarrow \boxed{x = -1}$$

substitute this into the first equation and solve for  $y$ .

$$-1 - y = 4 \longrightarrow -y = 4 + 1 \longrightarrow -y = 5 \longrightarrow \boxed{y = -5}$$

Check  $(-1, -5)$  with the second equation

$$-1 + (-5) = -6 \longrightarrow -6 = -6 \quad \underline{\text{TRUE}}$$

$\therefore$  the solution is  $(-1, -5)$

# FMPC 10

## 6.3, page 248

### #1a

FMPC 10 6.3 p.248

1a)  $y = -x + 2$  ①

$2x - y = 4$  ②

- In this system we see that  $y$  is already defined in equation ①

that is,  $y = -x + 2$

- We can use this definition of  $y$  and substitute it into equation ②

$$2x - y = 4$$

- We write equation ② as  $2x - (-x + 2) = 4$

- We solve this equation for  $x$  and get

$$2x + x - 2 = 4$$

$$3x - 2 = 4$$

$$3x = 4 + 2 \rightarrow 3x = 6 \rightarrow \boxed{x = 2}$$

- Substitute  $x = 2$  into either equation and solve for  $y$

Using equation ①  $y = -(2) + 2 \rightarrow \boxed{y = 0}$

CHECK  $(2, 0)$  with equation ②

$$2(2) - 0 = 4$$

$$4 = 4 \quad \text{TRUE}$$

$\therefore (2, 0)$  is the solution to this system



# FMPC 10

6.2, page 250

#2a

FMPC 10 6.3 p. 250

2a)  $y = 3x + 2$  ← slope,  $m = 3$

$y = kx + 2$  ← slope,  $m = k$

In order for this system to have one solution, the lines MUST have different slopes. Therefore  $k \neq 3$

# FMPC 10

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#2

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2. Let's call the numbers  $x$  and  $y$ .

$$x + y = 6 \quad \leftarrow \text{FROM THE FIRST SENTENCE}$$

$$x - y = 10 \quad \leftarrow \text{FROM THE SECOND SENTENCE}$$

$$2x = 16 \quad \text{ADDITION METHOD}$$

$$x = 8 \quad \text{substitute } x \text{ into first equation} \rightarrow \begin{aligned} 8 + y &= 6 \\ y &= 6 - 8 \\ y &= -2 \end{aligned}$$

CHECK to see if results are valid in second equation

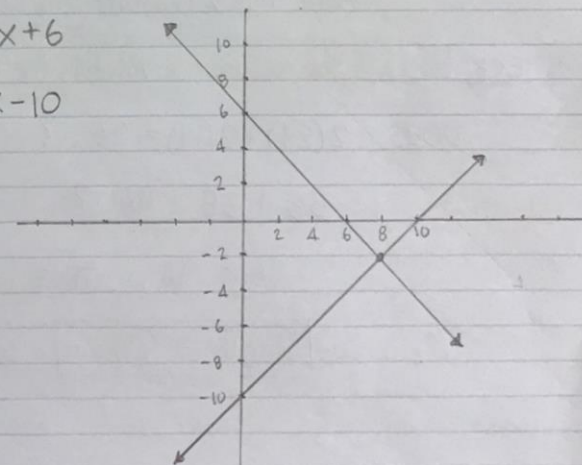
$$\text{DOES } 8 - (-2) = 10 \dots \text{YES!}$$

$\therefore$  the two numbers are  $x = 8$  and  $y = -2$

\* IF WE HAD SOLVE THIS QUESTION BY GRAPHING THE TWO EQUATIONS, IT WOULD LOOK LIKE THIS...

$$x + y = 6 \quad \longrightarrow \quad y = -x + 6$$

$$x - y = 10 \quad \longrightarrow \quad y = x - 10$$



The two lines intersect  
at  $(8, -2)$



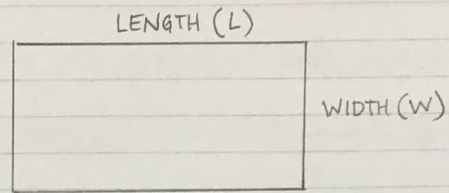
# FMPC 10

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#3

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3. Draw a rectangle



The first sentence tells us PERIMETER = 96  $\therefore 2L + 2W = 96$

second sentence tells us

$$L = W + 10$$

USE THE SUBSTITUTION METHOD

substitute the second equation into the first equation for L

$$2(W + 10) + 2W = 96$$

$$2W + 20 + 2W = 96$$

$$4W + 20 = 96$$

$$4W = 96 - 20$$

$$4W = 76 \longrightarrow W = 19 \text{ cm}$$

"PLUG" THIS VALUE INTO THE SECOND EQUATION  $L = 19 + 10 = 29 \text{ cm}$

CHECK to see if the results are valid in the first equation

$$\text{DOES } 2(29) + 2(19) = 96 \text{ ?}$$

$$58 + 38 = 96 \text{ ?}$$

$$96 = 96 \text{ TRUE}$$

$\therefore$  The length = 29 cm and the width = 19 cm

# FMPC 10

6.4, page 254

#6

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6. Let  $E$  represent Ellie's age and  $K$  represent Kate's age.

The first sentence tells us  $\longrightarrow E = 2K$  ①

The second sentence tells us  $\longrightarrow (K+7) + (E+7) = 20$

$$K + E + 14 = 20$$

$$K + E = 20 - 14$$

$$K + E = 6$$
 ②

Substitute ① into ② for  $E$   $\longrightarrow$

$$\begin{aligned} K + 2K &= 6 \\ 3K &= 6 \\ \boxed{K} &= \boxed{2} \end{aligned}$$

"PLUG"  $K=2$  INTO THE FIRST EQUATION  $\boxed{E = 2(2) = 4}$

CHECK using equation ②

DOES  $K + E = 6$  ?

$2 + 4 = 6$  ? TRUE

$\therefore$   $\boxed{\text{Ellie is 4 years old and Kate is 2 years old.}}$

# FMPC 10

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#7

FMPC 10 6.4 p.254

7. The question tells us

TOTAL COST = THE AMOUNT CHARGED FOR RENTING A TRUCK +  $y$  DOLLARS per KILOMETER

OR//  $C = x + y \cdot (\text{kilometers travelled})$

if the rental charge is

\$90 for 100 km then  $x + 100y = 90$  ①

\$110 for 150 km then  $x + 150y = 110$  ②

multiply eqn. ① by -1 and use the ADDITION method to solve this system

$$-x - 100y = -90 \quad \text{①} \times -1$$

$$x + 150y = 110 \quad \text{②}$$

$$50y = 20$$

$$y = \frac{\$20}{50 \text{ km}} = \$0.4/\text{km}$$

"PLUG" this value into ①  $x + 100(0.4) = 90$   
 $x + 40 = 90$   
 $x = 50$

CHECK using eqn ②

DOES  $50 + 150(0.4) = 110$  ?  
 $50 + 60 = 110$  TRUE ✓

$\therefore x = \$50$  and  $y = \$0.40/\text{km}$



# FMPC 10

6.4, page 255

#9

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9. Let's call the numbers  $x$  and  $y$

The first sentence says  $5x + 3y = 8$  ①

The second sentence says  $3x + 5y = 24$  ②

Multiply equation ① by  $-5$  and equation ② by  $3$  and then ADD the equations

$$-5 \times \text{①} \quad -25x - 15y = -40$$

$$3 \times \text{②} \quad \underline{9x + 15y = 72}$$

$$-16x = -32 \longrightarrow x = -2$$

"PLUG" this value into ①  $5(-2) + 3y = 8$

$$-10 + 3y = 8$$

$$3y = 8 + 10$$

$$3y = 18 \longrightarrow y = 6$$

CHECK using eqn. ②

DOES  $3(-2) + 5(6) = 24$  ?

$$-6 + 30 = 24 \quad \text{TRUE}$$

$\therefore$  the numbers are  $-2$  and  $6$

# FMPC 10

6.4, page 255

#10

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10. Let the number of dimes be  $d$ .

Let the number of quarters be  $q$ .

The first sentence tells us  $d + q = 80$  ①

The second sentence tells us  $0.1d + 0.25q = 15.20$  ②

because each dime  
is worth \$0.10

because each quarter  
is worth \$0.25

Rewrite eqn. ① as  $d = 80 - q$

Substitute for  $d$  into eqn. ②

$$\therefore 0.1(80 - q) + 0.25q = 15.20$$

$$8 - 0.1q + 0.25q = 15.20$$

$$8 + 0.15q = 15.20$$

$$0.15q = 15.20 - 8$$

$$0.15q = 7.20 \longrightarrow q = 48$$

"plug" this value into ①  $\longrightarrow d = 80 - 48 \longrightarrow d = 32$

CHECK using eqn ②

DOES  $0.1(32) + 0.25(48) = 15.20$  ?

$$3.2 + 12 = 15.20 \quad \text{TRUE}$$

$\therefore$  Jerry has 32 dimes and 48 quarters

# FMPC 10

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#12

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12. Let's call the amount of the first bottle A  
and the amount of the second bottle B

combining portions of both  $\rightarrow 8A + 15B = 12.2 \times 100$

the total volume is 100 ml  $\therefore A + B = 100$

Let's rewrite the first eqn. as  $8A + 15B = 1220$  ①  
second eqn. as  $B = 100 - A$  ②

Substitute ② into ① for B

$$\begin{aligned}8A + 15(100 - A) &= 1220 \\8A + 1500 - 15A &= 1220 \\1500 - 7A &= 1220 \\-7A &= 1220 - 1500 \\-7A &= -280 \\A &= 40 \text{ L}\end{aligned}$$

"PLUG"  $A = 40$  into ②  $\therefore B = 100 - 40 = 60 \text{ L}$

CHECK using eqn. ①

DOES  $8(40) + 15(60) = 1220$  ?

$320 + 900 = 1220$  TRUE

$\therefore$  You would need 40 L of 8% wine and 60 L of 15% wine to have 100 L of 12.2% wine.



# FMPC 10

6.4, page 256

#15

FMPC 10, 6.4 p.256

15. We need to use the equation  $\text{DISTANCE} = \text{RATE} \times \text{TIME}$   
Use example #2 (p.252) to help set this up.

We will use  $x$  as the speed of the plane  
and  $y$  as the wind speed

	SPEED (km/h)	TIME (h)	DISTANCE (km)
with wind	$x + y$	7	2835
against wind	$x - y$	7	1827

USING  $D = RT$  we get  $(x + y)(7) = 2835$

$$(x - y)(7) = 1827$$

$$\therefore 7x + 7y = 2835 \quad (1)$$

USING ADDITION METHOD  $7x - 7y = 1827 \quad (2)$

$$14x = 4662 \longrightarrow x = 333 \text{ km/h}$$

"PLUG" this into (1)  $\longrightarrow 7(333) + 7y = 2835$

$$2331 + 7y = 2835$$

$$7y = 2835 - 2331$$

$$7y = 504 \longrightarrow y = 72 \text{ km/h}$$

CHECK using eqn. (2)

DOES  $7(333) - 7(72) = 1827 ?$

$$2331 - 504 = 1827$$

$$1827 = 1827 \quad \text{TRUE}$$

$\therefore$  The speed of the plane is 333 km/h and wind speed is 72 km/h

# FMPC 10

6.4, page 256

#17

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17.	SPEED (km/h)	TIME (h)	DISTANCE (km)
CAR	$x+16$	$t$	480
TRUCK	$x$	$t$	400

- let the speed of the truck be  $x$   
the speed of the car be  $x+16$  (from the second sentence)
- The first sentence tells us both vehicles travel for the same amount of time

Since  $d = rt$

this means that  $(x+16)t = 480$

and  $xt = 400$  ①

∴  $xt + 16t = 480$  ②

multiply eqn. ① by  $-1$  and ADD both equations

$$-xt = -400$$

$$\underline{xt + 16t = 480}$$

$$16t = 80 \longrightarrow t = 5 \text{ hrs.}$$

"PLUG" this into eqn. ①  $\longrightarrow x(5 \text{ hrs}) = 400 \text{ km} \longrightarrow \boxed{x = 80 \frac{\text{km}}{\text{h}}}$

CHECK using eqn. ②

DOES  $(80)(5) + 16(5) = 480$  ?  
 $400 + 80 = 480$  TRUE

∴ the speed of the truck is  $80 \text{ km/h}$

# FMPC 10

6.5, page 261

#2a

FMPC 10 6.5 p.261

2a) To find the first term, let  $n=1$   $\therefore 1^2-2 = 1-2 = -1$

second term, let  $n=2$   $\therefore 2^2-2 = 4-2 = 2$

third term, let  $n=3$   $\therefore 3^2-2 = 9-2 = 7$

fourth term, let  $n=4$   $\therefore 4^2-2 = 16-2 = 14$

We see the first four terms of the sequence

$\{n^2-2\}$  are  $\boxed{-1, 2, 7, 14}$



# FMPC 10

6.5, page 261

#3a

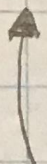
3a) Since the denominator of each fraction is increasing by 1 incrementally, I suspect the  $n^{\text{th}}$  term is  $\frac{1}{n}$   
just as the second term is  $\frac{1}{2}$  and the third term  $\frac{1}{3} \dots$

# FMPC 10

6.5, page 261

#4a

$$4. \quad a=4, \quad t_n = 2 + t_{n-1}$$



this statement is telling us that the value of ANY term in the sequence is determined by adding 2 to the previous term.

In this case, the first term is 4. This means the next term is  $4+2=6$  and the following term is  $6+2=8$  which makes the last term  $= 8+2=10$

so, 4, 6, 8, 10 are the first 4 terms.



# FMPC 10

6.5, page 261

#4c

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4c)  $a = 2$  this is the first term

$a_2 = 3$  this is the second term

if  $a_n = a_{n-1} + a_{n-2}$  then  $a_3 = a_{3-1} + a_{3-2}$

$$a_3 = a_2 + a_1 = 3 + 2 = 5$$

and  $a_4 = a_{4-1} + a_{4-2}$

$$a_4 = a_3 + a_2 = 5 + 3 = 8$$

the first 4 terms of the recursive sequence are

2, 3, 5, 8



# FMPC 10

6.5, page 262

#5a-f

FMPC 10 6.5 p.262.

$$5a) \sum_{k=1}^5 4 = 4 + 4 + 4 + 4 + 4 = 20$$

$$\begin{aligned} b) \sum_{k=1}^4 (k^2 - 2) &= (1^2 - 2) + (2^2 - 2) + (3^2 - 2) + (4^2 - 2) \\ &= (1 - 2) + (4 - 2) + (9 - 2) + (16 - 2) \\ &= (-1) + 2 + 7 + 14 = 22 \end{aligned}$$

$$\begin{aligned} c) \sum_{k=2}^5 (k^2 - 1) &= (2^2 - 1) + (3^2 - 1) + (4^2 - 1) + (5^2 - 1) \\ &= (4 - 1) + (9 - 1) + (16 - 1) + (25 - 1) \\ &= 3 + 8 + 15 + 24 = 50 \end{aligned}$$

$$\begin{aligned} d) \sum_{k=0}^3 (k^3 - 1) &= (0^3 - 1) + (1^3 - 1) + (2^3 - 1) + (3^3 - 1) \\ &= (0 - 1) + (1 - 1) + (8 - 1) + (27 - 1) \\ &= (-1) + 0 + 7 + 26 = 32 \end{aligned}$$

$$\begin{aligned} e) \sum_{k=1}^4 \frac{k^2}{2} &= \left(\frac{1^2}{2}\right) + \left(\frac{2^2}{2}\right) + \left(\frac{3^2}{2}\right) + \left(\frac{4^2}{2}\right) \\ &= \frac{1}{2} + \frac{4}{2} + \frac{9}{2} + \frac{16}{2} = \frac{30}{2} = 15 \end{aligned}$$

$$\begin{aligned} f) \sum_{k=6}^8 (k+1)^2 &= (6+1)^2 + (7+1)^2 + (8+1)^2 \\ &= 7^2 + 8^2 + 9^2 \\ &= 49 + 64 + 81 = 194 \end{aligned}$$

# FMPC 10

6.5, page 262

#8b

FMPC 10 6.5, p.262

8b) If  $a = \frac{2}{3}$  and  $d = -\frac{1}{4}$  then for  $t_n$ ,  $n=9$

$$\therefore t_9 = \frac{2}{3} + (9-1)\left(-\frac{1}{4}\right)$$

$$= \frac{2}{3} + (8)\left(-\frac{1}{4}\right)$$

$$= \frac{2}{3} - \frac{8}{4}$$

$$= \frac{2}{3} - 2$$

$$\text{but } 2 = \frac{6}{3}$$

$$t_9 = \frac{2}{3} - \frac{6}{3} = \boxed{-\frac{4}{3}}$$



# FMPC 10

6.5, page 263

#10a

$$10a) \quad t_6 = 10 \quad \text{and} \quad t_{18} = 46$$

$18 - 6 = 12$  differences between the 6<sup>th</sup> and 18<sup>th</sup> terms

$$\therefore 10 + 12d = 46$$

$$12d = 46 - 10$$

$$12d = 36$$

$$d = 3$$

The number of differences between the first term and the sixth term is  $6 - 1 = 5$  differences

$$\therefore a + 5d = 10 \quad \text{but } d = 3$$

$$a + 5(3) = 10$$

$$a = 10 - 15$$

$$a = -5$$



# FMPC 10

6.5, page 263

#11a

11a

$$\begin{array}{c} x+3, 2x+1, 5x+2 \\ \underbrace{\quad\quad}_d \quad \underbrace{\quad\quad}_d \end{array}$$

$$x+3+d=2x+1 \quad \underline{\text{and}} \quad 2x+1+d=5x+2$$

$$d=2x-x-3+1$$

$$\underline{d=x-2}$$

$$d=5x+2-2x-1$$

$$\underline{d=3x+1}$$

$$\therefore x-2=3x+1 \quad \text{because both} = d$$

$$-2-1=3x-x$$

$$-3=2x$$

$$\boxed{-\frac{3}{2}=x}$$

# FMPC 10

6.5, page 263

#11e

FMPC 10 6.5, page 263

11e) If  $x+4$ ,  $x^2+5$ , and  $x+30$  are consecutive terms of an Arithmetic Sequence

Then  $x^2+5 - (x+4) = x+30 - (x^2+5)$  because the common difference between each consecutive term is equal

$$\therefore x^2+5 - x - 4 = x+30 - x^2 - 5$$

$$x^2 - x + 1 = -x^2 + x + 25$$

let's move everything to the left side

$$x^2 - x + 1 + x^2 - x - 25 = 0$$

$$2x^2 - 2x - 24 = 0 \quad \text{factor out 2}$$

$$2(x^2 - x - 12) = 0 \quad \text{if } 2A = 0 \text{ then } A = 0$$

$$\therefore x^2 - x - 12 = 0$$

$$(x-4)(x+3) = 0$$

$$x-4=0 \quad \text{OR} \quad x+3=0$$

$$\therefore \boxed{x=4} \quad \text{OR} \quad \boxed{x=-3}$$

# FMPC 10

6.6, page 268

#1a,c,i

FMPC 10 6.6, p.268

1a) Use  $S_n = \frac{n}{2}(a+l)$  where  $a=3$ ,  $l=2n+1$  and  $n=n$

$$\begin{aligned}\therefore S_n &= \frac{n}{2}(3+(2n+1)) = \frac{n}{2}(3+2n+1) = \frac{n}{2}(2n+4) \\ &= \frac{2n^2+4n}{2} \\ &= \boxed{n^2+2n}\end{aligned}$$

c) ① We know  $a=2$  and  $l=77$  but we don't know how many terms are in the series. We need to find  $n$  using

$$t_n = a + (n-1)d \quad \text{where } t_n=77, a=2, \text{ and } d=3$$

$$\therefore 77 = 2 + (n-1)3 \longrightarrow 77 = 2 + 3n - 3$$

$$77 = 3n - 1 \longrightarrow 78 = 3n \longrightarrow n = 26$$

$$\therefore \textcircled{2} S_{26} = \frac{26}{2}(2+77) = 13(79) = \boxed{1027}$$

i) ①  $a = \frac{1}{2}$ ,  $l = \frac{55}{8}$ . Find the number of terms in the series

using  $t_n = a + (n-1)d$  where  $t_n = \frac{55}{8}$ ,  $a = \frac{1}{2}$

$$d = \frac{7}{8} - \frac{1}{2} = \frac{7}{8} - \frac{4}{8} = \frac{3}{8}$$

$$\frac{55}{8} = \frac{1}{2} + (n-1)\frac{3}{8} \longrightarrow \frac{55}{8} = \frac{1}{2} + \frac{3}{8}n - \frac{3}{8}$$

$$\frac{55}{8} = \frac{4}{8} + \frac{3n}{8} - \frac{3}{8} \longrightarrow 55 = 4 + 3n - 3$$

$$55 = 1 + 3n \longrightarrow 54 = 3n \longrightarrow n = 18$$

$$\textcircled{2} S_{18} = \frac{18}{2}\left(\frac{1}{2} + \frac{55}{8}\right) \longrightarrow S_{18} = 9\left(\frac{4}{8} + \frac{55}{8}\right) = 9\left(\frac{59}{8}\right) = \boxed{\frac{531}{8}}$$



# FMPC 10

6.6, page 269

#2a,c,i

FMPC 10 6.6, p. 269

$$2a) S_{20} = \frac{20}{2}(8+65) = 10(73) = \boxed{730}$$

c) ① Determine the value of the first term,  $a$ , using

$$t_n = a + (n-1)d \quad \text{where } t_{56} = 13, n = 56 \text{ and } d = -9$$

$$\therefore 13 = a + (56-1)(-9) \longrightarrow 13 = a + (55)(-9)$$

$$13 = a - 495 \longrightarrow 495 + 13 = a \longrightarrow \underline{a = 508}$$

② Using  $S_n = \frac{n}{2}(a+l)$

$$S_{56} = \frac{56}{2}(508+13) = 28(521) = \boxed{14588}$$

i) ① Find  $d$  first. There are  $15-5 = 10$  differences between  $a_5$  and  $a_{15}$

$$\therefore a_5 + 10d = a_{15}$$

$$42 + 10d = -18 \longrightarrow 10d = -18 - 42 \longrightarrow 10d = -60 \longrightarrow \underline{d = -6}$$

② Find  $a$  using  $t_n = a + (n-1)d$  where  $t_5 = 42$ ,  $d = -6$  and  $n = 5$

$$\therefore 42 = a + (5-1)(-6) \longrightarrow 42 = a + (4)(-6) \longrightarrow 42 = a - 24$$

$$42 + 24 = a \longrightarrow \underline{a = 66}$$

③ Find  $S_{40}$  using  $S_n = \frac{n}{2}(2a + (n-1)d)$  where  $n = 40$ ,  $a = 66$   
 $d = -6$

$$\begin{aligned} \therefore S_{40} &= \frac{40}{2}(2(66) + (40-1)(-6)) = 20(132 + (39)(-6)) \\ &= 20(132 - 234) \\ &= 20(-102) \\ &= \boxed{-2040} \end{aligned}$$



# FMPC 10

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#5a

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$$5a) \sum_{x=2}^b (23-2x) = 91 \quad \text{The number of terms in this series is } b-2+1 = b-1$$

List a few terms of this series to see what it looks like

$$a = 23 - 2(2) = 23 - 4 = 19 \quad \leftarrow \text{THE FIRST TERM}$$

$$a_2 = 23 - 2(3) = 23 - 6 = 17$$

$$a_3 = 23 - 2(4) = 23 - 8 = 15$$

The series looks like this  $19 + 17 + 15 + \dots + (23 - 2b) = 91$

$a_1 \quad a_2 \quad a_3 \quad \dots \quad a_b$

THE LAST TERM

Use  $S_n = \frac{n}{2}(a+l)$  where  $a=19$ ,  $l=23-2b$ ,  $n=b-1$

$$\therefore 91 = \frac{b-1}{2}(19+23-2b) \quad \text{and } S_{b-1} = 91$$

$$91 = \frac{b-1}{2}(42-2b)$$

$$2 \times 91 = (b-1)(42-2b)$$

$$182 = 42b - 2b^2 - 42 + 2b$$

$$182 = -2b^2 + 44b - 42$$

$$0 = -2b^2 + 44b - 42 - 182$$

$$0 = -2b^2 + 44b - 224$$

$$0 = -2(b^2 - 22b + 112)$$

$$\therefore 0 = b^2 - 22b + 112$$

$$0 = (b-8)(b-14)$$

$$\therefore b=8 \quad \text{or} \quad b=14$$

PRODUCT	SUM
+112	-22
-2 -56	-58
-4 -28	-32
-8 -14	-22 ✓



# FMPC 10

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#8

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$$8. \quad a = 1491, \quad d = -7, \quad S_n = 0, \quad n = n$$

Use the formula  $S_n = \frac{n}{2} (2a + (n-1)d)$

$$\therefore 0 = \frac{n}{2} (2(1491) + (n-1)(-7))$$

$$0 = \frac{n}{2} (2982 - 7n + 7)$$

$$0 = \frac{n}{2} (2989 - 7n)$$

$$0 = \frac{2989n}{2} - \frac{7n^2}{2} \quad \text{mult. each term by 2}$$

$$0 = 2989n - 7n^2 \quad \text{divide both terms by 7}$$

$$0 = 427n - n^2 \quad \text{factor out } n$$

$$0 = n(427 - n)$$

$$\therefore n = 0 \quad \text{or} \quad n = 427$$

# FMPC 10

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#9, 10, 12

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9.  $a=8, d=4, n=50$

$$\begin{aligned} \text{Use } t_n &= a + (n-1)d \quad \therefore t_{50} = 8 + (50-1)4 \\ &= 8 + (49)(4) \\ &= \boxed{204 \text{ seats}} \end{aligned}$$

10.  $a=1000, d=100, n=19$  use  $S_n = \frac{n}{2}(2a + (n-1)d)$

$$\begin{aligned} S_{18} &= \frac{19}{2}(2(1000) + (19-1)(100)) \\ &= \frac{19}{2}(2000 + (18)(100)) = \frac{19}{2}(2000 + 1800) = \frac{19}{2}(3800) = \boxed{\$36100} \end{aligned}$$

\* on the child's 18<sup>th</sup> birthday, the child has received 19 deposits.

12. Let's call the terms  $x, x+d,$  and  $x+2d$

$$\text{We are told } x + (x+d) + (x+2d) = 3 \longrightarrow 3x + 3d = 3 \rightarrow \boxed{x+d=1}$$

$$\text{and } x^2 + (x+d)^2 + (x+2d)^2 = 75 \quad \boxed{x=1-d}$$

$$\therefore x^2 + (x+d)(x+d) + (x+2d)(x+2d) = 75$$

$$x^2 + x^2 + 2xd + d^2 + x^2 + 4xd + 4d^2 = 75$$

$$3x^2 + 6xd + 5d^2 = 75 \quad \text{sub } x=1-d$$

$$3(1-d)^2 + 6(1-d)d + 5d^2 = 75$$

$$3(1-d)(1-d) + 6d - 6d^2 + 5d^2 = 75$$

$$3(1-2d+d^2) + 6d - d^2 = 75$$

$$3 - 6d + 3d^2 + 6d - d^2 = 75$$

$$2d^2 + 3 = 75$$

$$2d^2 = 72$$

$$d^2 = 36$$

$$d = +6 \quad \text{or} \quad d = -6$$

$$\therefore x = 1-6 \quad \text{or} \quad x = 1-(-6)$$

$$= -5 \quad \text{or} \quad = 7$$

The terms are

$$\boxed{-5, 1, 7} \quad \text{or} \quad \boxed{7, 1, -5}$$