

## Ch. 2 Practice Test

## Solutions

1. D.

Break  $y = f(3x - 6)$  down to  $y = f(3(x - 2))$ . From this we can see a horizontal compression by a factor of  $\frac{1}{3}$  and a horizontal translation of 2 units RIGHT.

2. C.

If  $(6, -5)$  is a point on  $y = f(x)$  then for  $y = -f(2(x + 2)) - 3$  there is a

- Reflection in the x-axis (y is replaced with  $-y$ )
  - Horizontal compression by a factor of  $\frac{1}{2}$
  - Horizontal translation 2 units LEFT
  - Vertical translation 3 units DOWN
- |           |                   |          |
|-----------|-------------------|----------|
| $(6, -5)$ | $\longrightarrow$ | $(6, 5)$ |
| $(6, 5)$  | $\longrightarrow$ | $(3, 5)$ |
| $(3, 5)$  | $\longrightarrow$ | $(1, 5)$ |
| $(1, 5)$  | $\longrightarrow$ | $(1, 2)$ |

3. B.

$$y = f(2x + 10) \longrightarrow y = f(2(x + 5))$$

- Horizontal compression by a factor of  $\frac{1}{2}$
  - Horizontal translation 5 units LEFT
- |           |                   |            |
|-----------|-------------------|------------|
| $(4, -3)$ | $\longrightarrow$ | $(2, -3)$  |
| $(2, -3)$ | $\longrightarrow$ | $(-3, -3)$ |

4. C.

Horizontal translation 5 units LEFT so  $(a, b) \longrightarrow (a-5, b)$   
Vertical translation 1 unit DOWN so  $(a-5, b) \longrightarrow (a-5, b-1)$

5. D.

Horizontal translation 2 units LEFT  
Vertical translation 5 units DOWN

6. B.

$$y = \frac{1}{3}x - 7 \longrightarrow x = \frac{1}{3}y - 7 \longrightarrow x + 7 = \frac{1}{3}y \longrightarrow 3(x + 7) = y$$

$$3x + 21 = y \longrightarrow f^{-1}(x) = 3x + 21$$

7. A.

$$y = f(x) \xrightarrow{\text{horiz. comp.}} y = f(3x) \xrightarrow{\text{horiz. translation}} y = f(3(x+2)) \xrightarrow{\quad} y = f(3x+6)$$

8. B.

$$y = \sqrt{x} \xrightarrow{\text{horiz. Comp}} y = \sqrt{\frac{1}{4}x} \xrightarrow{\text{horiz. translation}} y = \sqrt{\frac{1}{4}(x-3)}$$

9. C.

$$\begin{aligned} y = -f(2x) + 3 & \text{ shows a reflection in the x-axis } (4, -5) \xrightarrow{\quad} (4, 5) \\ & \text{ a horiz. comp. by a factor of } \frac{1}{2} \quad (4, 5) \xrightarrow{\quad} (2, 5) \\ & \text{ and a vert. trans. 3 units UP } \quad (2, 5) \xrightarrow{\quad} (2, 8) \end{aligned}$$

10. B.

Two things have happened with this graph

- It has been reflected in the y-axis (replace  $x$  with  $-x$ )
- It has *then* been translated 8 units RIGHT (replace  $x$  with  $x-8$ )

11. C.

$4y = f(-x)$  represents a vertical compression of a factor of  $\frac{1}{4}$

which means  $(6, -12)$  becomes  $(6, -3)$  and since  $x$  has been replaced with  $(-x)$   
 $(6, -3)$  becomes  **$(-6, -3)$**

12. B.

Two things have happened with this graph

- It has been horizontally expanded by a factor of 2 (replace  $x$  with  $\frac{1}{2}x$ )
- It has *then* been translated 1 unit RIGHT (replace  $x$  with  $x-1$ )

13. D.

Following the order given:

$(9, -12)$  becomes  $(27, -12)$

$(27, -12)$  becomes  $(27, 12)$

$(27, 12)$  becomes  $(27, 7)$

$(27, 7)$  becomes  $(7, 27)$

14. C or D.

The inverse of  $y = x^2$  is  $x = y^2$

Isolate this for y and get  $y = \sqrt{x}$  but,  $\sqrt{x} = x^{1/2}$

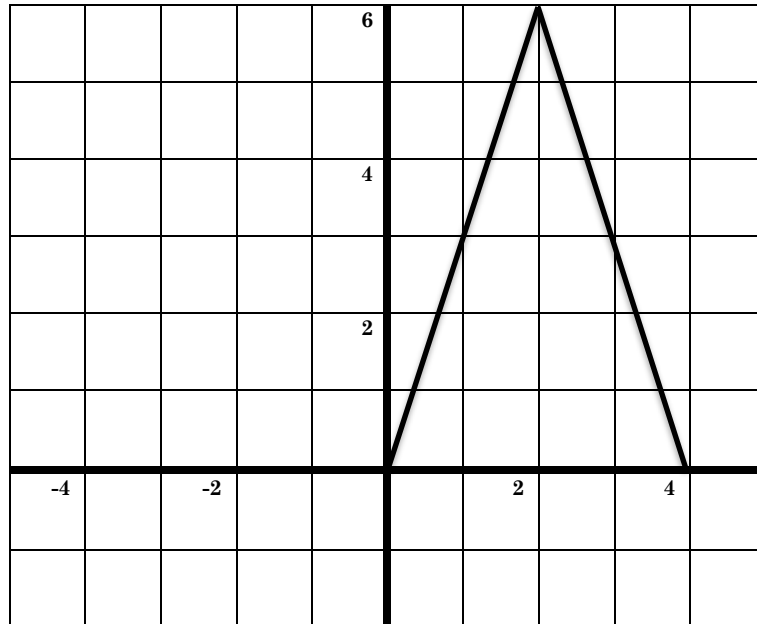
So,.... $y = x^{1/2}$

15. C.

$$f(x) = 2x + 3 \longrightarrow y = 2x + 3 \longrightarrow x = 2y + 3 \longrightarrow x - 3 = 2y$$

$$\frac{x-3}{2} = y \longrightarrow f^{-1}(x) = \frac{x-3}{2}$$

16.

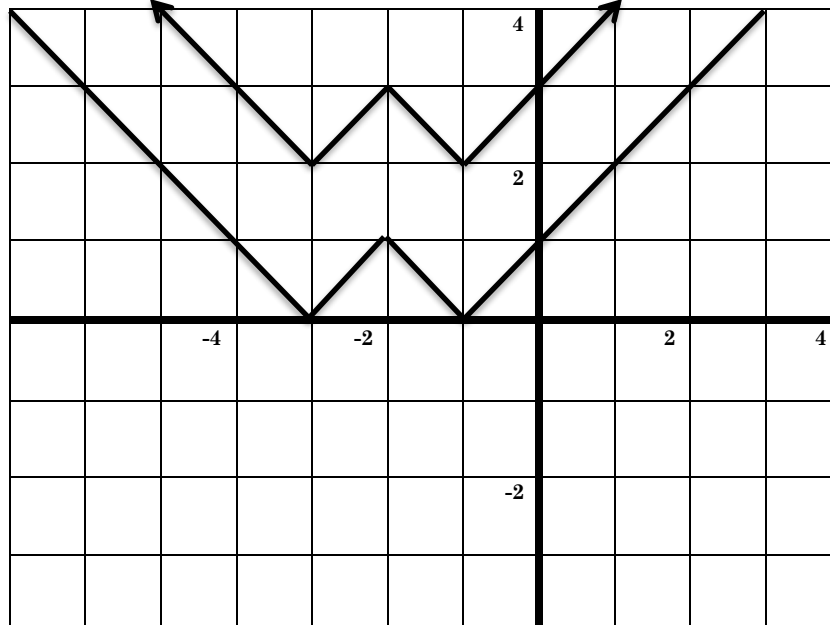


The vertical expansion by a factor of 3 transforms the point (0, 2) to (0, 6).

Next, the horizontal translation 2 units right transforms (0, 6) to (2, 6)

The points (-2, 0) and (2, 0), at the base, move to (0, 0) and (4, 0) respectively

17.



**First: Reflect the portion of the graph below the x-axis, above the x-axis.**

**Second: Translate the graph 2 units UP**

18. The y-coordinate is only affected. The vertical expansion by a factor of 2 transforms the point to (6, 20). The reciprocal of the function simply requires us to take the reciprocal of the y-coordinate which gives us  **$(6, \frac{1}{20})$**

19.

Two things have happened with this graph

- It has been horizontally compressed by a factor of  $\frac{1}{2}$  (replace x with 2x)

$$y = f(2x)$$

- It has *then* been translated 3 units RIGHT (replace x with x-3)

$$y = f(2(x-3))$$

The final equation would be  **$y = f(2x-6)$**

20.

The solution is obtained by work “backwards”.

If (2, -8) is on the graph of  $y = f(x-3) + 4$ , then the x-coordinate and y-coordinate on  $y = f(x)$  are (2-3, -8-4)  $\longrightarrow$   **$(-1, -12)$**

$y = f(x)$  underwent a horizontal translation of 3 units left so we must move 3 units right to determine the original x-coordinate  
 $y = f(x)$  underwent a vertical translation of 4 units up so we must move 4 units down to determine the original y-coordinate

21.

A maximum value on  $y = f(x)$  represents the y-coordinate. For  $y = \frac{1}{3} f(\frac{1}{2} x)$  the y-coordinate undergoes a vertical compression by a factor of  $\frac{1}{3}$ .

Therefore the maximum value of  $y = \frac{1}{3} f(\frac{1}{2} x)$  is **3**.

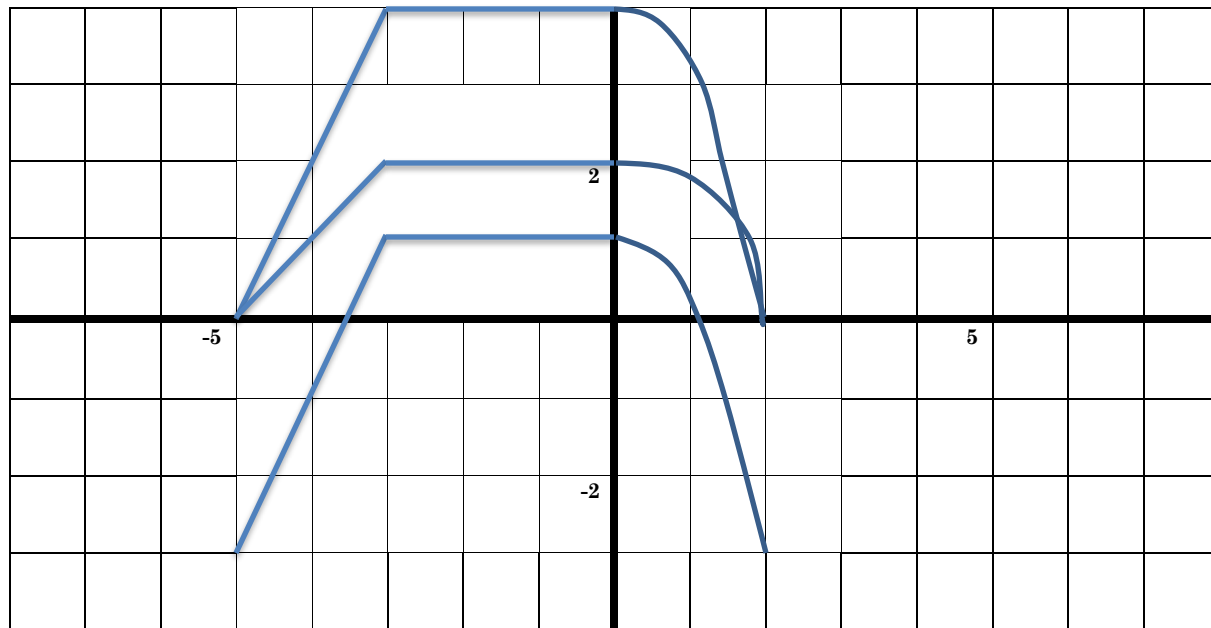
22.

$$f(x) = \frac{3x}{x+1} \longrightarrow y = \frac{3x}{x+1} \longrightarrow x = \frac{3y}{y+1} \longrightarrow x(y+1) = 3y$$

$$xy + x = 3y \longrightarrow x = 3y - xy \longrightarrow x = y(3 - x) \longrightarrow \frac{x}{3-x} = y$$

$$f^{-1}(x) = \frac{x}{3-x}$$

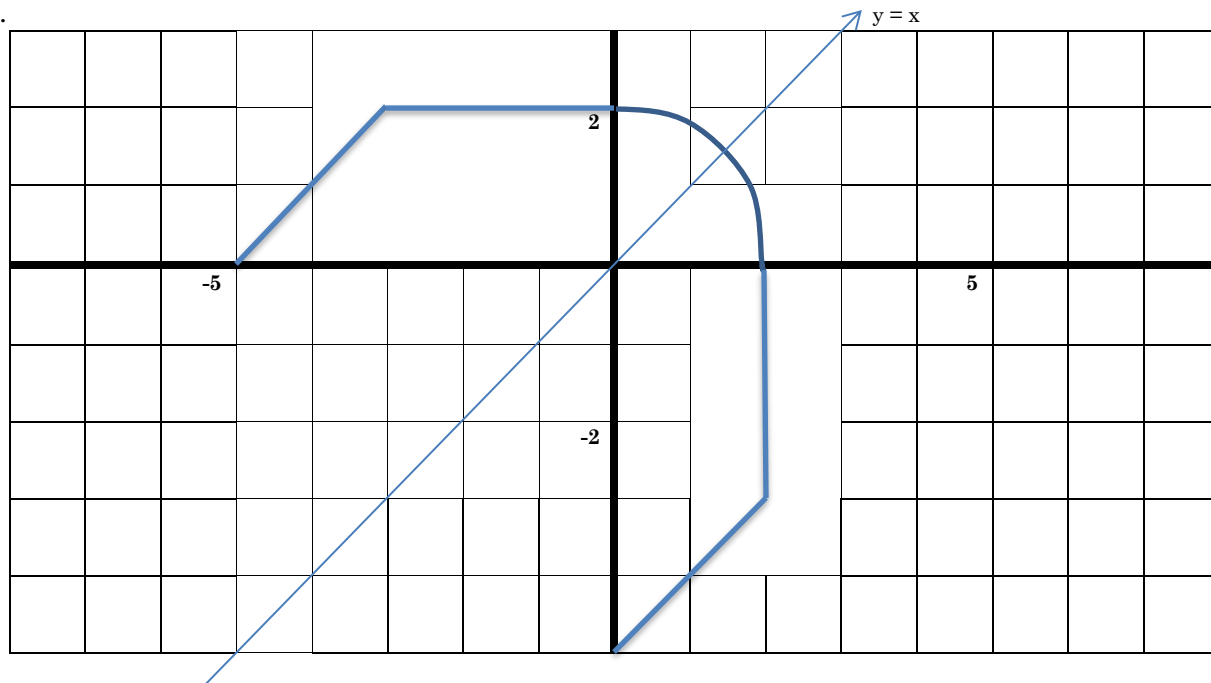
23.



**First: Vertically expand the shape by a factor of 2**

**Second: Vertically translate the shape 3 units DOWN.**

24.



Reflect the graph in the line  $y = x$ . This can be done by switching the x and y coordinates of key points and then plot them.

$(-5, 0)$  reflects to  $(0, -5)$

$(-3, 2)$  reflects to  $(2, -3)$

$(0, 2)$  reflects to  $(2, 0)$

$(2, 0)$  reflects to  $(0, 2)$ .....and then we connect the dots.